



Goa, India

The Quark-Gluon Plasma

An Overview

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1. Introduction: States of Matter

The Classical Approach of Physics:

- what are the basic constituents of matter and their interactions?
- what are the states of matter these interactions can produce?
- what are the transitions between these states of matter?

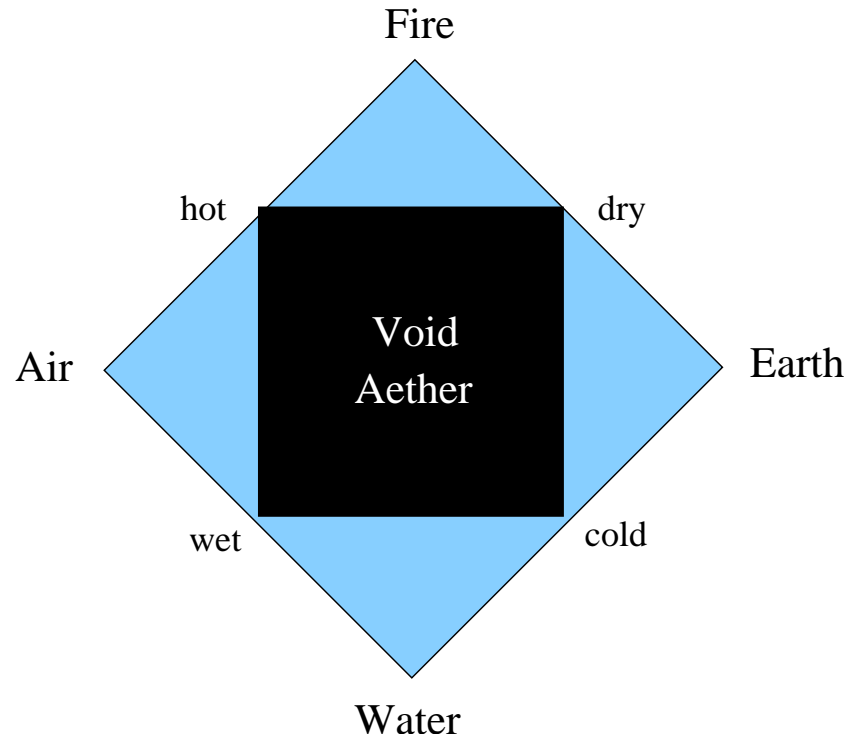
New Physics:

- \exists general pattern of collective behavior
- different constituents, interactions \sim similar states of matter
- critical behavior has universal scale structure

What are the states of matter in the world we see?

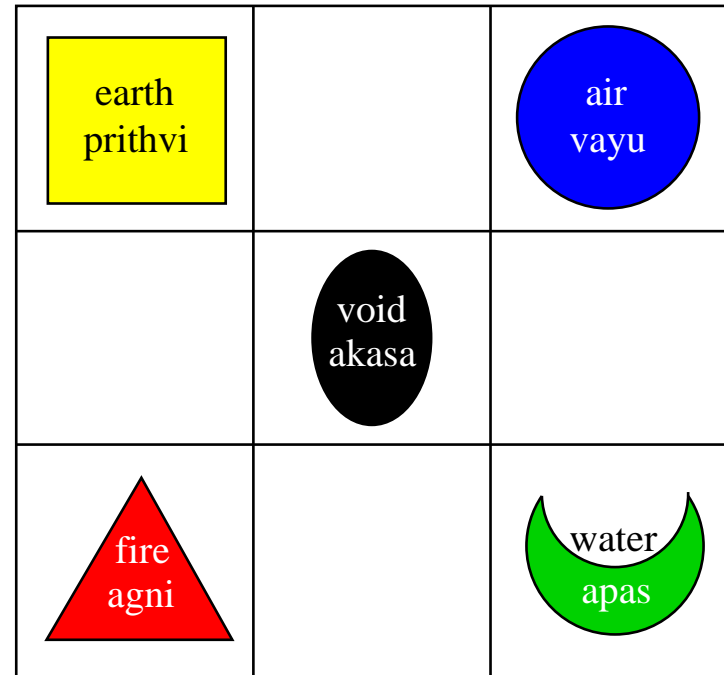
The States of Matter

early Greek (500 B. C.)



void = quintessence

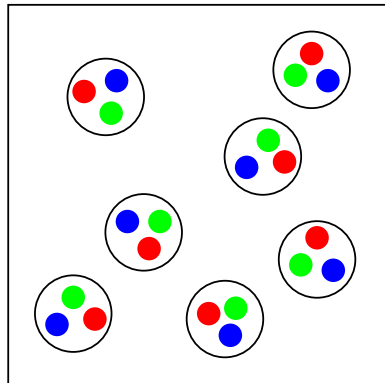
early Hindu (500 B. C.)



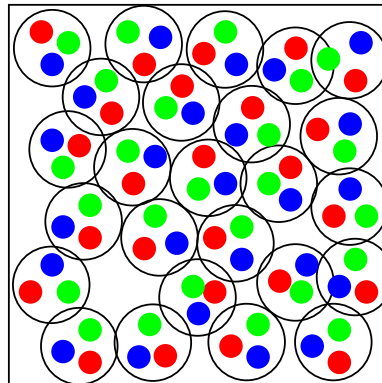
pancha mahabhuta

What is the Quark-Gluon Plasma?

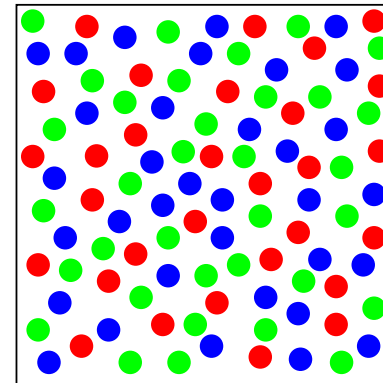
A state of strongly interacting **matter**, in which the **constituents** of hadrons, quarks and gluons, are **not spatially confined** to form color-neutral **bound states**.



Nucleon Gas



Nuclear Matter



Quark Matter

When many hadrons overlap, quarks cannot identify “their hadron”, the concepts of a hadron and of confinement become meaningless, color screening and high quark density (asymptotic freedom) forbid hadronic scales \Rightarrow transition to a new state of matter

Confined Matter

- quark-antiquark pairs or three-quark states form **color-neutral states** of **hadronic size** ~ 1 fm;
- quarks acquire a dynamically generated “effective” mass of about 300 MeV by gluon dressing \rightarrow spontaneous **chiral symmetry breaking**;
- mesonic matter: constituents are mesons and baryons, the interaction is **resonance-dominanted**;
- baryonic matter: constituents are nucleons, the interaction is **long-range attraction** (1 fm) and **short range repulsion** (0.5 fm)

increasing the meson density (by increasing T), or increasing the nucleon density (by compressing nuclear matter) leads to hadron overlap and thus deconfinement.

what happens in the deconfinement transition?

Deconfined Matter

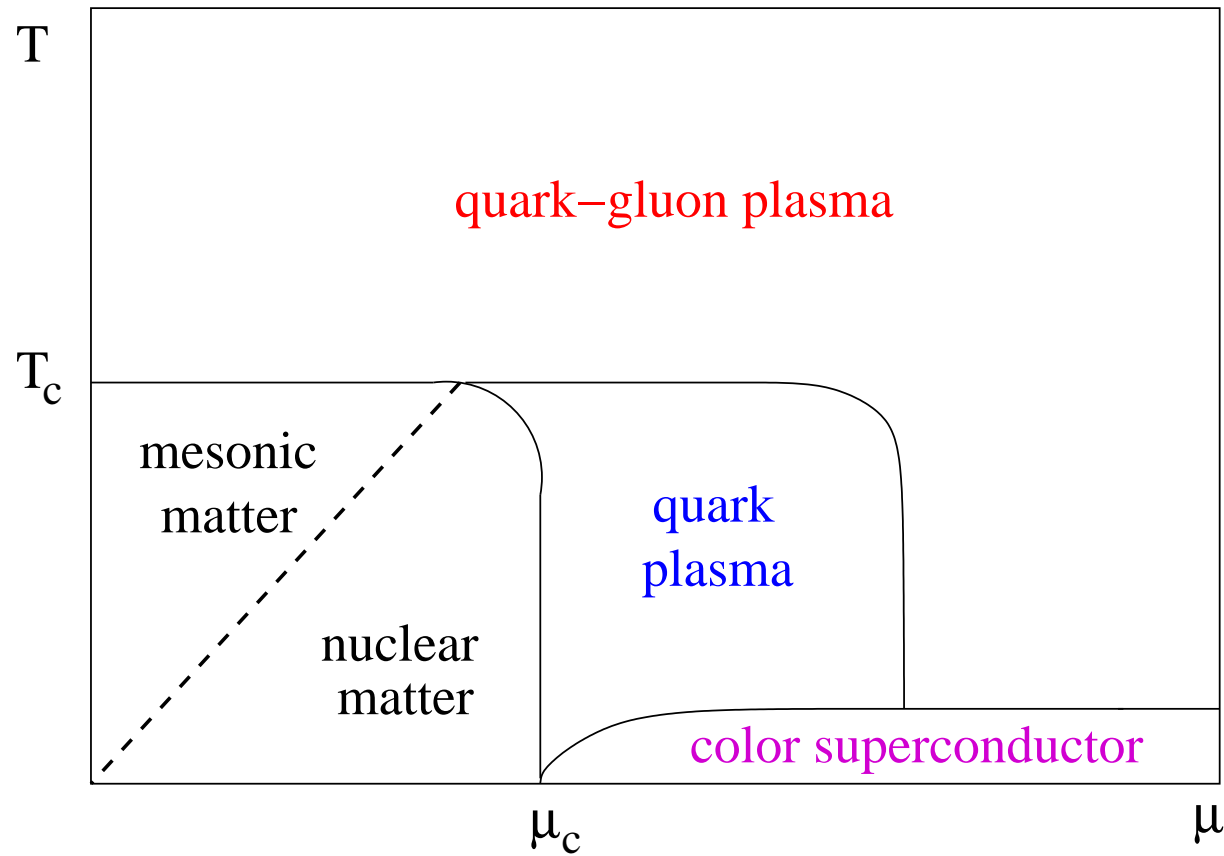
- at deconfinement, bound states are dissolved, constituents are colored quarks; \Rightarrow **insulator-conductor transition** of QCD
- the gluon dressing melts, the quark mass drops to Lagrangian mass; \Rightarrow **chiral symmetry restoration**.

do the two phenomena coincide?

In general: either yes or first deconfinement, then chiral symmetry restoration [Banks & Casher 1979]

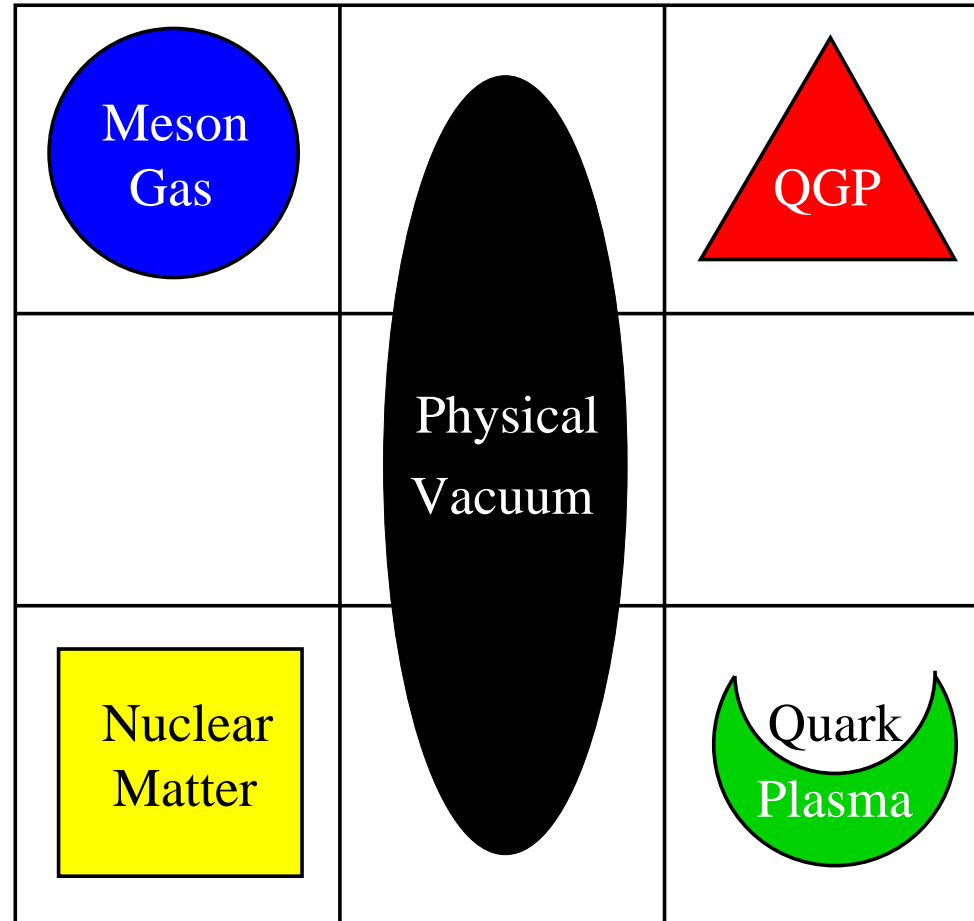
- possible state of deconfined massive colored quarks: **quark plasma**;
lattice studies: at low baryon density, deconfinement and chiral symmetry restoration coincide;
- deconfined quarks (whether massive or not) may still interact;
QCD \Rightarrow quark-quark binding \Rightarrow **colored bosonic diquarks**;
- colored diquark bosons at low T can form Bose condensate: **color superconductor**.

Speculative phase diagram for strongly interacting matter:



NB: in all phases, \exists interactions!

restate in Hindu form:



now turn to **QGP**

2. From Hadrons to Quarks and Gluons

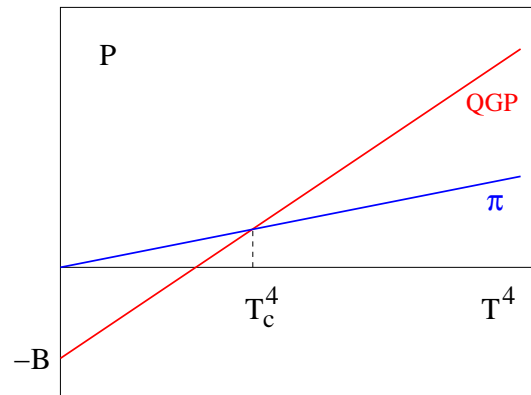
simplest confined matter: ideal pion gas $P_\pi = \frac{\pi^2}{90} 3 T^4 \simeq \frac{1}{3} T^4$

simplest deconfined matter: ideal quark-gluon plasma

$$P_{QGP} = \frac{\pi^2}{90} \left\{ 2 \times 8 + \frac{7}{8} [2 \times 2 \times 2 \times 3] \right\} T^4 - B \simeq 4 T^4 - B$$

with bag pressure B for outside/inside vacuum

given $P_\pi(T)$ vs. $P_{QGP}(T)$: nature chooses highest P (lowest F)



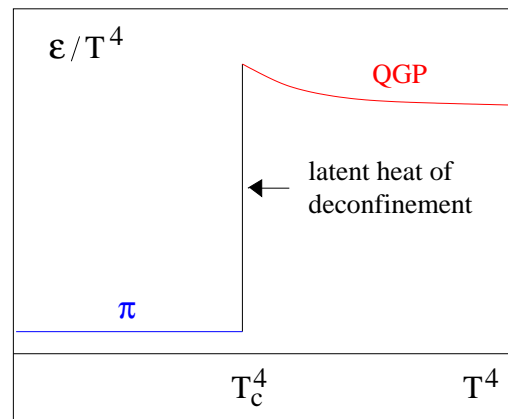
phase transition from hadronic matter at low T to QGP at high T
critical temperature:

$$P_\pi = P_{QGP} \rightarrow T_c^4 \simeq 0.3 B \simeq 150 \text{ MeV}$$

with $B^{1/4} \simeq 200 \text{ MeV}$ from quarkonium spectroscopy

corresponding energy densities

$$\epsilon_\pi \simeq T^4 \rightarrow \epsilon_{QGP} \simeq 12 T^4 + B$$



at T_c , energy density changes abruptly by latent heat of deconfinement

compare energy density and pressure:

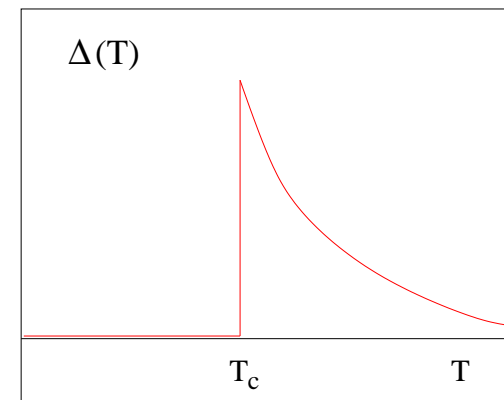
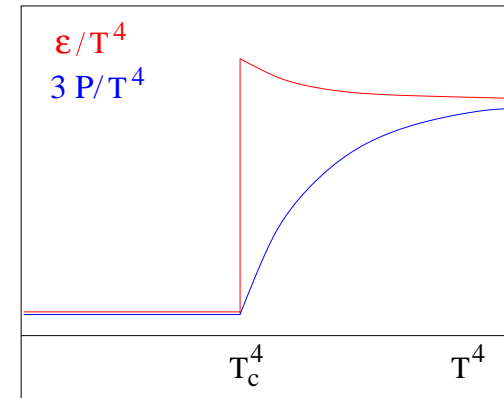
ideal gas $\epsilon = 3P$

here we obtain

and the interaction measure

$$\Delta \equiv \frac{\epsilon - 3P}{T^4} = \frac{4B}{T^4}$$

shows that for $T_c \leq T < 2 - 3 T_c$
the **QGP** is strongly interacting



so far, simplistic model; real world?

3. Finite Temperature Lattice QCD

given QCD as **dynamics** input, calculate resulting **thermodynamics**, based on **QCD partition function**

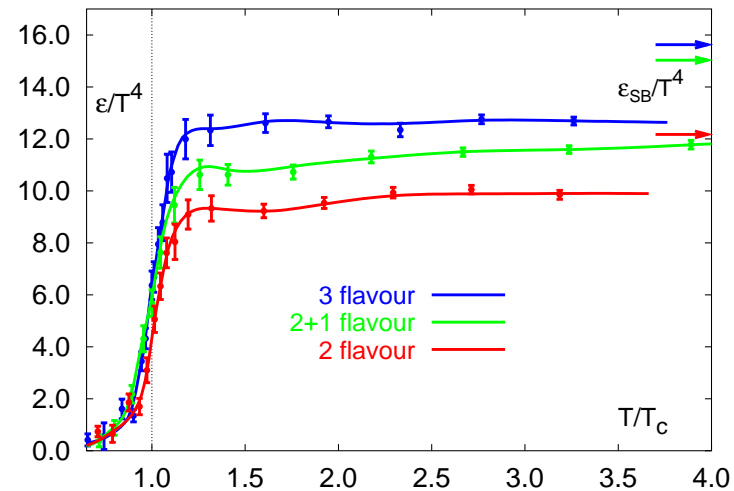
⇒ **lattice regularization, computer simulation**

- energy density

⇒ **latent heat of deconfinement**

For $N_f = 2, 2 + 1$:

$$T_c \simeq 175 \text{ MeV}$$
$$\epsilon(T_c) \simeq 0.5 - 1.0 \text{ GeV/fm}^3$$



explicit relation to deconfinement, chiral symmetry restoration?

⇒ order parameters

- deconfinement

$$\Rightarrow m_q \rightarrow \infty$$

Polyakov loop $L(T) \sim \exp\{-F_{Q\bar{Q}}/T\}$

$F_{Q\bar{Q}}$: free energy of $Q\bar{Q}$ pair for $r \rightarrow \infty$

$$L(T) \begin{cases} = 0 & T < T_L \text{ confinement} \\ \neq 0 & T > T_L \text{ deconfinement} \end{cases}$$

variation defines deconfinement temperature T_L

- chiral symmetry restoration $\Rightarrow m_q \rightarrow 0$

chiral condensate $\chi(T) \equiv \langle \bar{\psi}\psi \rangle \sim M_q$

measures dynamically generated ('constituent') quark mass

$$\chi(T) \begin{cases} \neq 0 & T < T_\chi \text{ chiral symmetry broken} \\ = 0 & T > T_\chi \text{ chiral symmetry restored} \end{cases}$$

variation defines chiral symmetry temperature T_χ

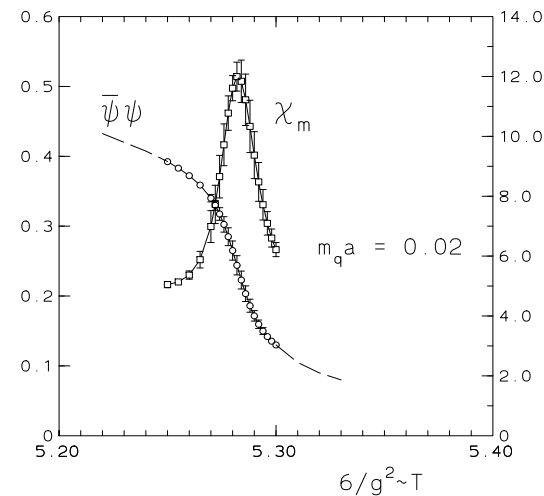
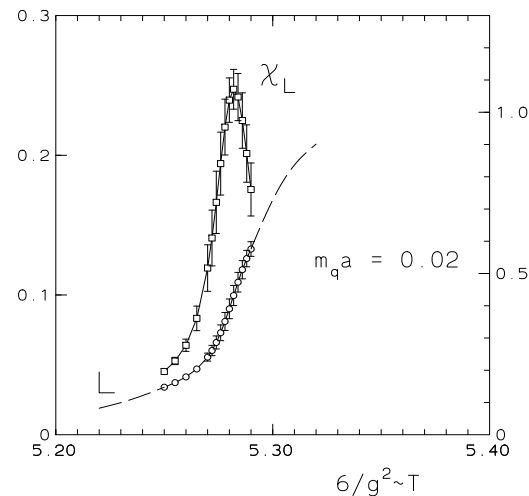
- how are T_L and T_χ related?

$SU(N)$ gauge theory: \sim spontaneous Z_N breaking at T_L

QCD, chiral limit: \sim explicit Z_N breaking by $\chi(T) \rightarrow 0$ at T_χ

chiral symmetry restoration \Rightarrow deconfinement

lattice results



Polyakov loop & chiral condensate vs. temperature

at $\mu = 0$, \exists one transition hadronic matter \rightarrow QGP

for $N_f = 2$, $m_q \rightarrow 0$ at $T_c = T_L = T_\chi \simeq 175$ MeV

Finite temperature lattice QCD shows:

- \exists transition at $T \sim 0.175 \pm ? \text{ GeV}$, where deconfinement & chiral symmetry restoration coincide
- at transition, ϵ increases suddenly by latent heat of deconfinement

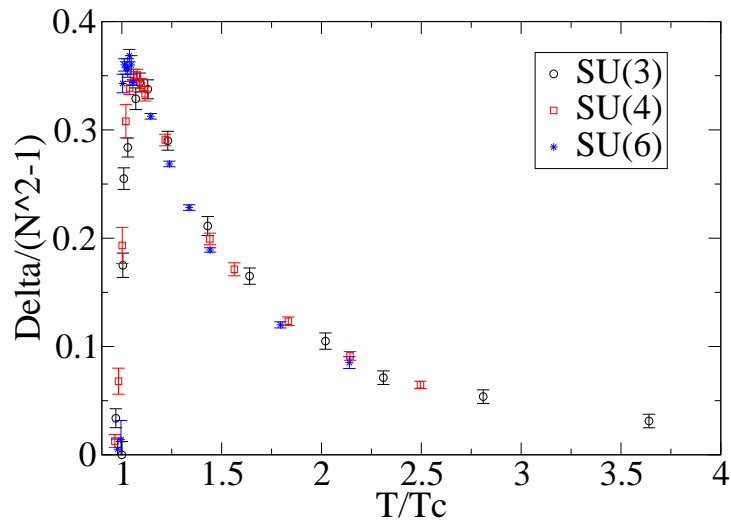
What about interactions in QGP?

interaction measure(trace of energy-momentum tensor)

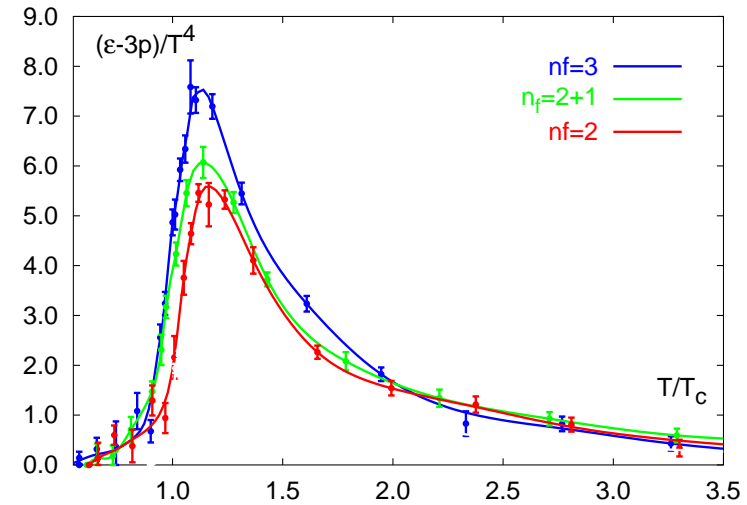
$$\Delta = \frac{\epsilon - 3P}{T^4}$$

vanishes for non-interacting massless constituents

quarks and gluons are (ideally) massless; what $\Delta(T > T_c)$?



Datta & Gupta 2009



Karsch, Laermann & Peikert 2000

4. The Strongly Interacting QGP

Expect that for high enough T , asymptotic freedom \rightarrow ideal QGP
(perturbation theory)

how high is enough? – consider best known case $SU(3)$ gauge theory

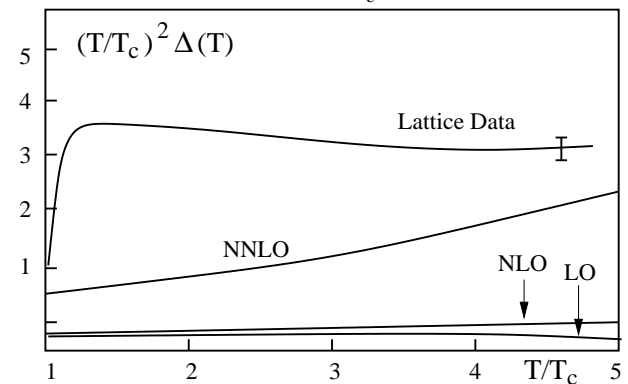
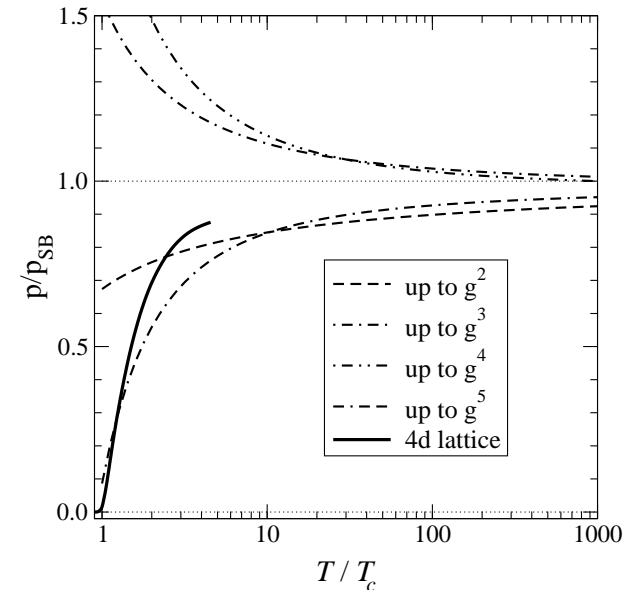
\exists perturbative calculations up to $O(g^5)$

perturbation theory oscillates strongly
does not converge for $T \leq 10 T_c$

non-pert. extension [Kajantie et al. 2003]:
still qualitatively wrong for $T \leq 5 T_c$

re-organize perturbation theory
(“re-summed” theory, HTL)
[Andersen, Strickland & Su 2010]

- weak coupling approaches cannot account for QGP at
 $T \leq T_c \leq 5 T_c$: no dip at T_c , wrong (log) T -dependence



Non-perturbative approach: bag model

non-interacting quarks & gluons in “medium” gluon condensate

$$\Delta = \frac{4B}{T^4} = \frac{G_0^2}{T^4}$$

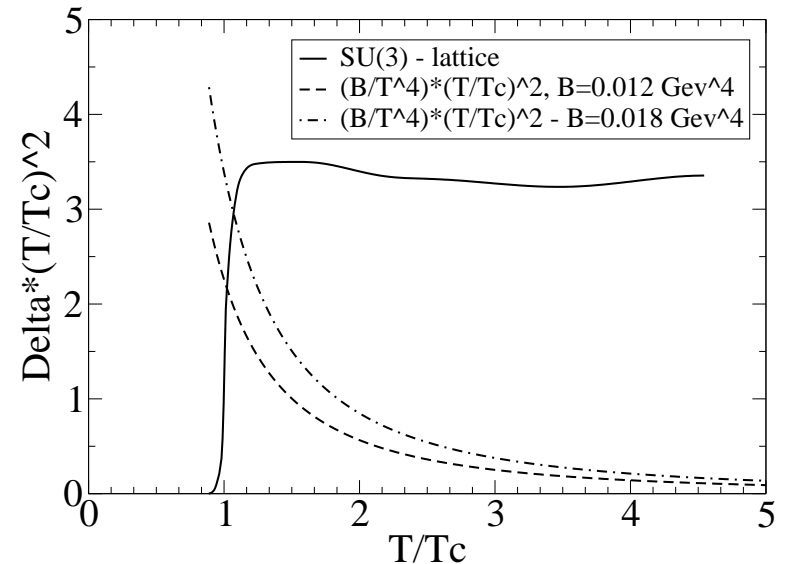
bag pressure \sim gluon condensate
at $T = 0$

numerical estimate $G_0^2 \simeq 0.012 \text{ GeV}^4$
[Shifman, Vainshtein & Zakharov 1979]

Conclude:

- weak coupling: T -dependence too weak, no dip at T_c
- bag model: T -dependence too strong, no dip at T_c

what is happening in QGP for $T \geq T_c$?



∃ two regions

- critical region as $T \rightarrow T_c$, “singular” behavior
- screening region in hot QGP

consider gluons in deconfined medium:

polarization → dressing, effective gluon mass

- as $T \rightarrow T_c$ from above, correlation length increases/diverges,
so gluon polarizes more & more of medium
- as $T > T_c$ increases, correlation length decreases, so gluon
sees less and less of medium
- as $T > T_c$ increases, energy density of medium increases

two competing effects:

consider $SU(2)$ gauge theory

⇒ continuous transition, critical exponents

[Goloviznin & HS 1993]

for $T \rightarrow T_c$, with $t \equiv (T/T_c)$,

- energy density $\epsilon \sim (t - 1)^{1-\alpha}$
- correlation volume $V_{cor} \sim (t - 1)^{-2\nu-\eta}$

with (Z_2 universality class) $\alpha = 0.11$, $\nu = 0.69$, $\eta = 0.04$, so that

$$m_{crit}(T) \sim \epsilon V_{cor} \sim (t - 1)^{1-\alpha-2\nu-\eta} \sim (t - 1)^{-0.41}$$

effective gluon mass diverges for $T \rightarrow T_c$

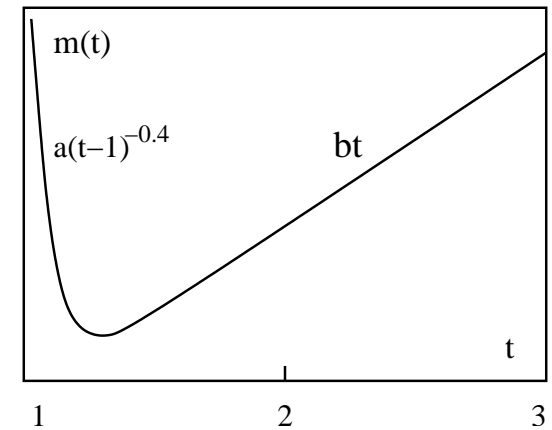
in hot QGP, screening length $r_D \sim 1/T$, hence

- $\epsilon \sim T^4$
- $V_{cor} \sim T^{-3}$
- $m_{crit}(T) \sim \epsilon V_{cor} \sim T$

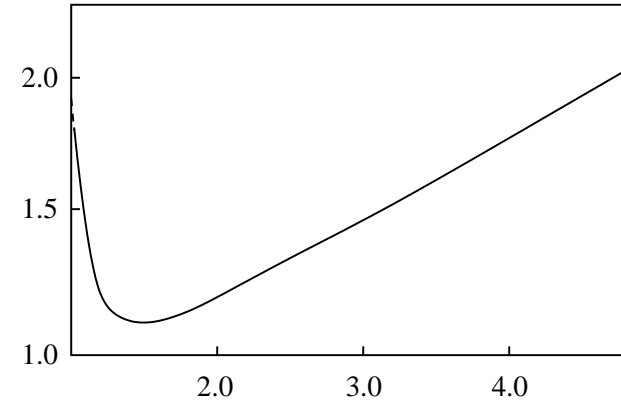
overall behavior of effective gluon mass

$$m(T) = a(t - 1)^{-c} + bt$$

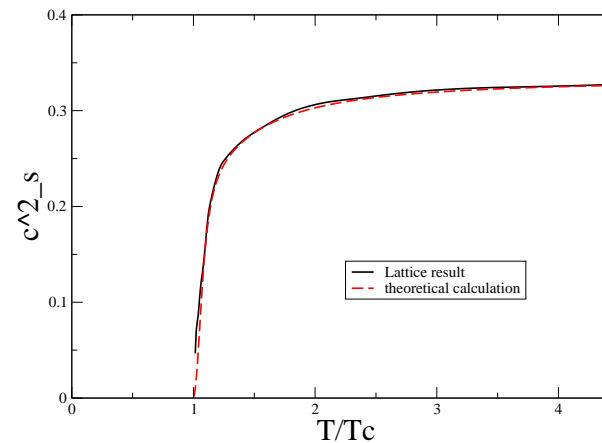
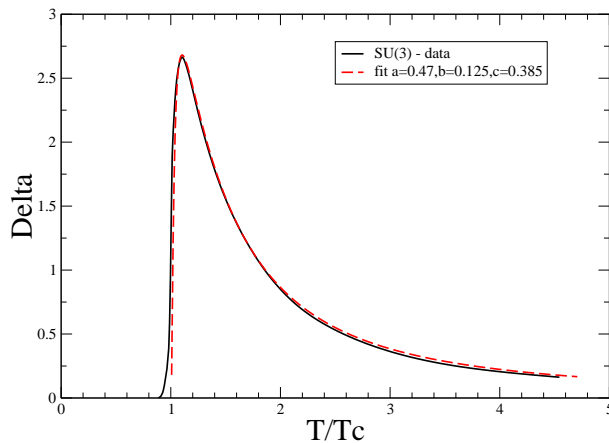
with constants a, b, c ; here $c = 0.41$



retain this form in general
apply to $SU(3)$ gauge theory
[Castorina, Miller & HS 2010]



excellent description of all thermodynamic quantities, including $\Delta(T)$
NB: speed of sound in QGP “vanishes” at T_c , heavy gluons...



5. Probing the Quark-Gluon Plasma

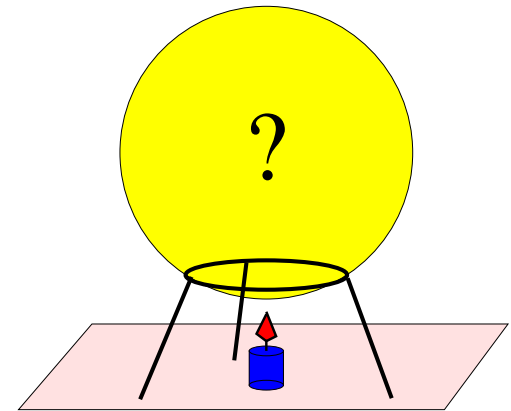
At high temperatures and/or densities, strongly interacting matter becomes a QGP;

how can we probe its properties and its behaviour as function of temperature and density?

Given a volume of strongly interacting matter and an energy source, how can we determine its state at different temperatures?

NB:

equilibrium thermodynamics, no collision effects, time dependence, equilibration, etc.



- Possible probes:
- hadron radiation
 - electromagnetic radiation
 - dissociation of quarkonium states
 - energy loss of parton beams

Here, just a brief first look....

The medium is **hotter** than its environment (vacuum) and hence emits

- Hadron Radiation

emission of light hadrons

(made of u, d, s quarks)

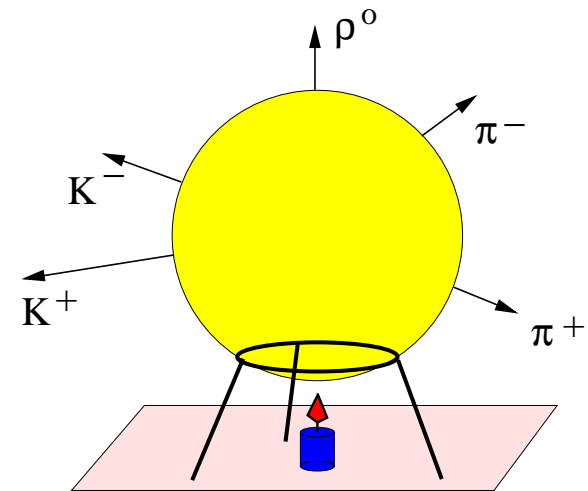
scale $\sim 1 \text{ fm} \simeq 1/(200 \text{ MeV})$

cannot exist in hot interior

emission at surface of $T \simeq T_c$

information about hadronization stage

\Rightarrow same relative abundances for different initial energy densities



Hadron emission: no information about pre-hadronic medium

BUT:

if medium not contained,
it can expand freely

⇒ Hydrodynamic Flow

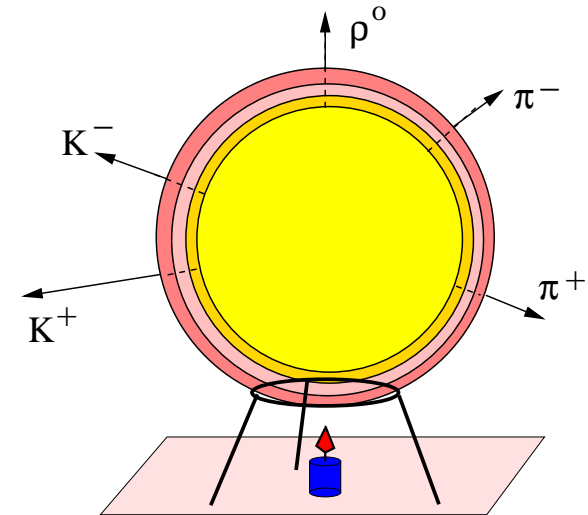
- “radial flow”: boosts hadron momenta

non-spherical initial state (peripheral collisions)

⇒ spatially different pressure gradients

- “directed” or “elliptic” flow, boost depends on spatial directions

both forms of flow depend on conditions of medium in all stages and hence can (in principle) also provide information about hot QGP



In the interior of the medium, quark-gluon interactions or quark-antiquark annihilation leads to

- Electromagnetic Radiation

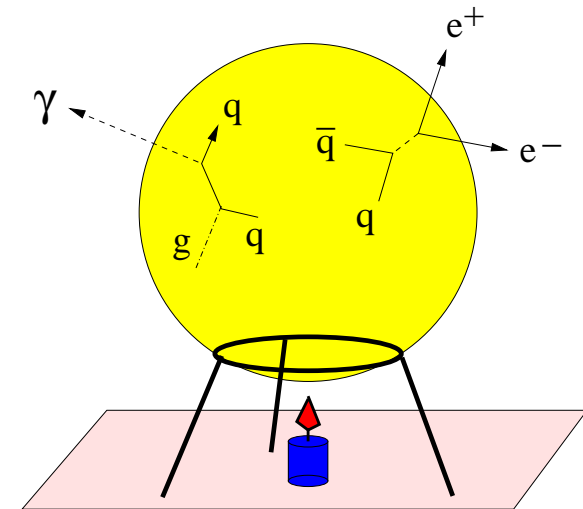
produced photons and dileptons

leave medium without further interaction

provide information about the medium

at the time of their production:

probe of hot QGP



problem:

they can be formed anywhere & at any time

even at the surface or by the emitted hadrons

task: identify hot thermal radiation

hadronic and e-m radiation: emitted by the medium itself

provide information about the medium at the time of production

other possibility: “outside” probes

- Quarkonium Suppression

quarkonia: bound states of heavy quarks ($c\bar{c}$, $b\bar{b}$)

smaller than usual hadrons ($r_Q \ll r_h \simeq 1$ fm),

binding energies 0.5 – 1.0 GeV

\Rightarrow can survive in QGP

in some temperature range $T > T_c$

Example: charmonium states

$J/\psi(1S) - r_{J/\psi} \simeq 0.2$ fm

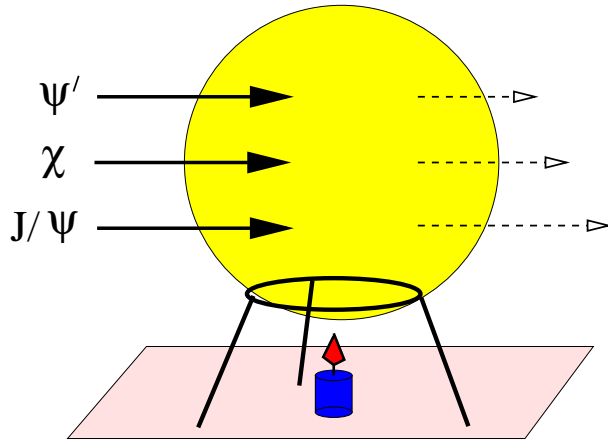
$\chi_c(1P) - r_\chi \simeq 0.3$ fm

$\psi'(2S) - r_{\psi'} \simeq 0.4$ fm

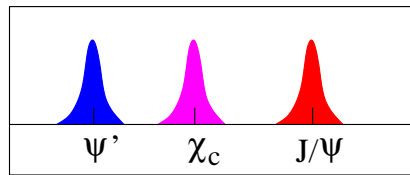
different charmonia “melt” in QGP at different temperatures

potential & lattice studies: $T_{\psi'} \simeq T_\chi \simeq 1 - 1.1$, $T_{J/\psi} \simeq 1.5 - 2 T_c$

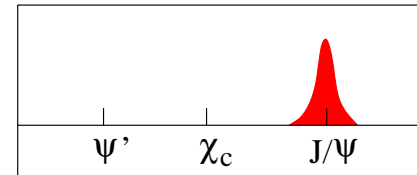
$\epsilon_{\psi'} \simeq \epsilon_\chi \simeq 1 - 1.5$, $\epsilon_{J/\psi} \simeq 8 - 12$ GeV/fm³



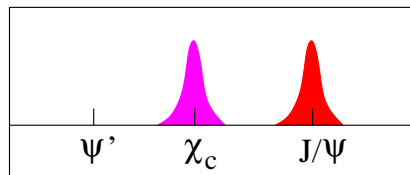
⇒ “sequential charmonium melting”
as quantitatively predicted
property of QGP



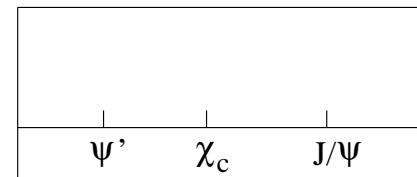
$T < T_c$



$T_\chi < T < T_\psi$



$T_{\psi'} < T < T_\chi$



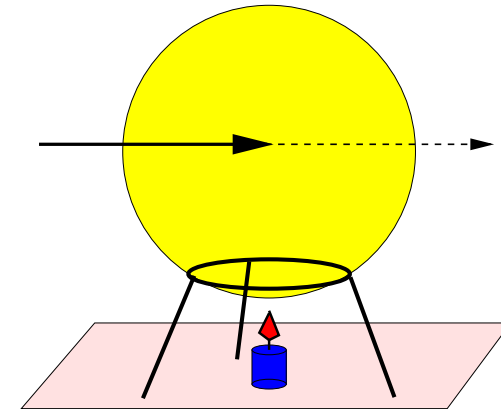
$T > T_\psi$

similar to solar spectra as thermometer of sun

- Jet Quenching

shoot an energetic parton beam
(quarks or gluons) into QGP,
measure energy of outgoing beam

attenuation (“quenching”)
determined by density of medium
increases with temperature



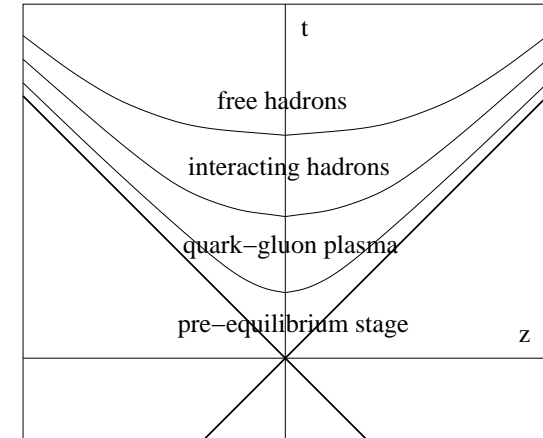
NB: how to get “external” probes in nuclear collision experiments?

- Hard Probes:

quarkonia, open charm/beauty, jets, energetic photons & dileptons
– formed very early in the collision, are present when QGP appears
– can be predicted (to large extent) by perturbative QCD
– can be “gauged” in pp and pA collisions

6. Three Questions to LHC Experiments

High energy nuclear collisions:
 initial hot deconfined medium
 expands, cools, hadronizes
 energy density of initial QGP
 Bjorken estimate: run film backwards



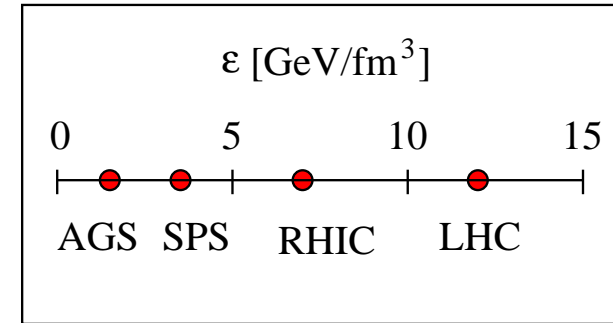
$$\epsilon(s) \simeq \frac{p_0}{\pi R_A^2 \tau} \left(\frac{dN_h}{dy} \right)_0^{AA}$$

Empirically, hadron multiplicity $\left(\frac{dN_h}{dy} \right)_0^{AA} \simeq A^\alpha \ln(\sqrt{s}/2m)$

so that for $A \simeq 200$, $\epsilon(s) \simeq 1.5 \ln(\sqrt{s}/2m)$

increase $\sqrt{s} \rightarrow$ increase multiplicity \rightarrow increase initial energy
 density

values model-dependent,
ratios not (very much)



hadronization at fixed energy density (transition value)

hotter initial medium must expand more → larger source size for
hadron emission

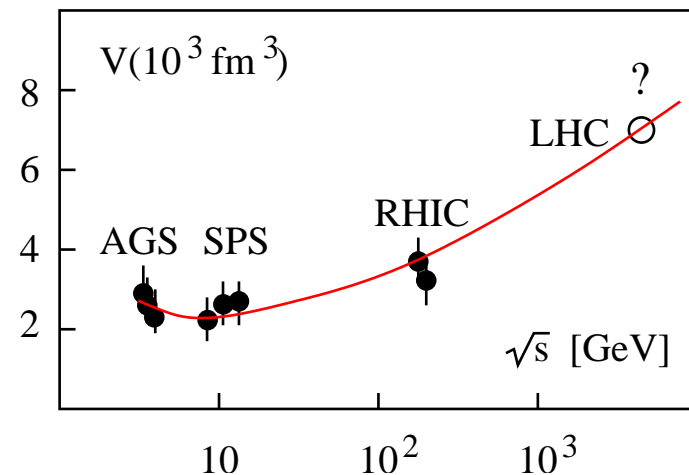
source size measurable:

HBT interferometry,

from astronomy (star size)

[Adamova et al. (CERES) 2002]

Q1: source size at LHC?

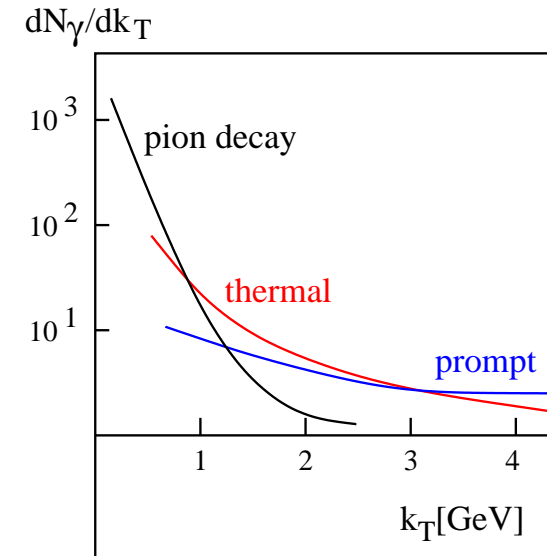


thermal photons $qg \rightarrow q\gamma$: internal thermometer
telling temperature T of medium

$$\frac{dN_\gamma}{dk_T} \sim \exp\{-k_T/T\}$$

problems:

- emission at all stages,
from hot QGP to hadron gas
- other sources: prompt (pre-QGP),
hadron decay
- window for $1 < k_T < 3$ GeV ?

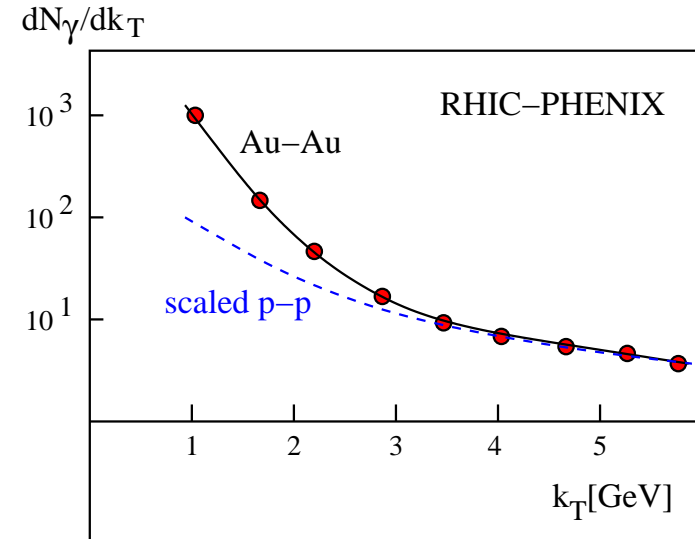


recent measurements from PHENIX collaboration at RHIC:
compare Au-Au (possible thermal photons) to scaled p-p data

thermal fit

$$T = 221 \pm 23(\text{stat}) \pm 18(\text{syst}) \text{ MeV}$$

above $T_c \simeq 170 \text{ MeV}$



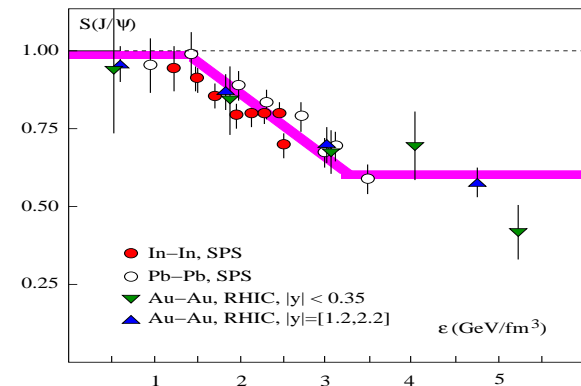
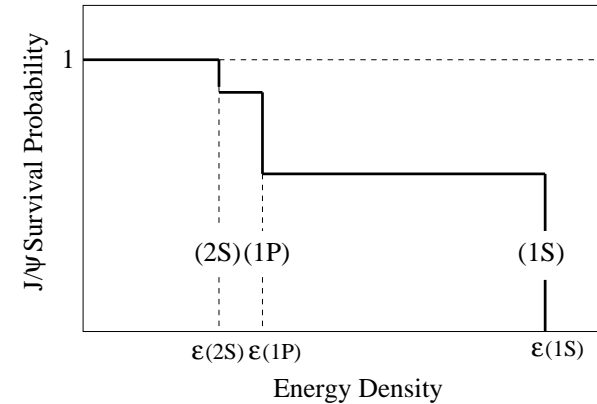
[Adare et al. (PHENIX) 2008]

Q2: thermal photon temperature at LHC?

Quarkonium states act as external thermometers of QGP
 produced before QGP, then dissolved (or not) by its presence
sequential melting specifies QGP energy density, temperature

first ψ' , then χ_c , then J/ψ
 direct J/ψ suppression
 for $\epsilon \geq 8 - 10 \text{ GeV}/\text{fm}^3$
 similar for bottomonium

present data:
 suppression onset at SPS
 same degree of suppression at RHIC
 (old data)



alternative scenario:

dominant charmonium production at hadronization stage

⇒ “statistical regeneration of charm”

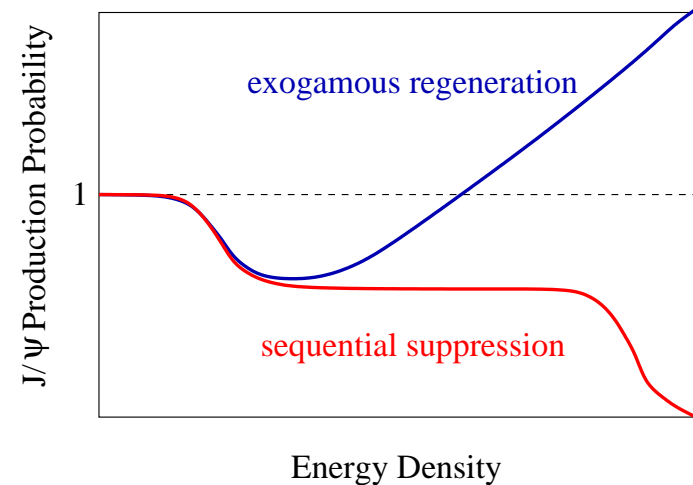
abundant charm quark production → J/ψ enhancement, not
suppression

sequential suppression:

direct experimental QCD test

statistical regeneration:

direct test of charm thermalization



Q3: J/ψ production at LHC: up or down?

corollary: Υ production at LHC?

Summary

In strong interaction thermodynamics \exists a well-defined transition at which

- **deconfinement** sets in & **chiral symmetry** is restored
- **latent heat** increases energy density
- transition temperature $T_c \simeq 160 - 190$ MeV.

For $T > T_c$, the state of matter is a plasma of deconfined quarks and gluons which can be probed by

- **electromagnetic radiation**
- **quarkonium spectra**
- **jet quenching**

Three essential questions for LHC experiments

- **source size** for hadron emission
- temperature for real/virtual **thermal photons**
- **quarkonium production** pattern